

Fuzzy solution of homogeneous heat equation having solution in Fourier series form

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Received: 5 July 2016 / Accepted: 21 August 2018
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Abstract While solving practical problems, we often come across situations where the system involves fuzziness. The mathematical models resulting in partial differential equations, involve fuzzy parameters and variables. In available literature, methods are presented mainly for solving non-homogeneous fuzzy partial differential equations (see Allahviranloo in *Comput Methods Appl Math* 2(3):233–242, 2002; Allahviranloo and Taheri in *Int J Contemp Math Sci* 4(3):105–114, 2009; Allahviranloo and Afshar in *Iran J Fuzzy Syst* 7(3):33–50, 2010; Allahviranloo et al. in *Appl Soft Comput* 11:2186–2192, 2011). We present a method to find the solution of homogeneous fuzzy heat equations with fuzzy Dirichlet boundary conditions. We consider the fuzziness in zero in the homogeneous equation as well as in the boundary conditions. The initial conditions are also in fuzzy form. Further, we study the solution of fuzzy heat equation when the fuzzy initial conditions are represent as a Fourier series.

Keywords Fuzzy heat equation · Seikkala solution · Fourier series

Mathematics Subject Classification 34A07 · 35K51

1 Introduction

Study of fuzzy partial differential equations (FPDEs) means the generalization of partial differential equations (PDEs) in fuzzy sense.

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